

**Lab 15: Spend some cycles thinking****17 April**

**Collaboration:** In lab, we encourage collaboration and discussion as you work through the problems. These activities, like recitation, are meant to get you to review what we've learned, look at problems from a different perspective and allow you to ask questions about topics you don't understand. We encourage discussing problems with your neighbors as you work through this lab!

**Setup:** Copy the lab code from our public directory to your private directory:

```
% cd private/15122
% cp -R /afs/andrew/course/15/122/misc/lab15 .
% cd lab15
```

You should add your code to the existing files `graph.c`, `graph-search.c`, `graph-search.h`, and `graph-test.c` in the directory `lab15`.

**Grading:** Finish through (2.d) for full credit, and finish (3.a) and (3.b) for extra credit.

**The graph interface**

This lab involves implementing a graph using an adjacency matrix rather than an array of adjacency lists. Graphs will be specified by the following C interface (as in `graph.h`):

```
typedef unsigned int vertex;
// typedef _____* graph_t;

// New graph with numvert vertices
graph graph_new(unsigned int numvert);
    //@ensures \result != NULL;

unsigned int graph_size(graph G);
    //@requires G != NULL;

bool graph_hasedge(graph G, vertex v, vertex w);
    //@requires G != NULL;
    //@requires v < graph_size(G) && w < graph_size(G);

void graph_addedge(graph G, vertex v, vertex w);
    //@requires G != NULL;
    //@requires v != w && v < graph_size(G) && w < graph_size(G);
    //@requires !graph_hasedge(G, v, w);

void graph_free(graph G);
    //@requires G != NULL;
```

**Representing undirected graphs with an adjacency matrix**

In class, we discussed the *adjacency list* implementation of graphs. In this lab, we'll work through the *adjacency matrix* implementation.

Recall that if a graph has  $n$  vertices, then its adjacency matrix `adj` is an  $n \times n$  array of booleans such that `adj[i][j]` is true if there is an edge from vertex  $i$  to vertex  $j$  (for valid  $i$  and  $j$ ), false otherwise.

Since the graph is undirected, if `adj[i][j]` is true, then `adj[j][i]` should also be true, and if `adj[i][j]` is false, then `adj[j][i]` should also be false. The graph should not have any self-loops (i.e., a vertex with an edge to itself).

(2.a) Complete the data structure invariant function `is_graph` that returns true if `G` points to a valid graph given the definition above, or false otherwise.

1pt

Make sure to capture the fact that the graph is undirected in your data structure invariant! Compare notes with a neighbor before you move on.

(2.b) Complete the `graph_new` function that creates a new graph using a dynamically-allocated 2D array of boolean for the adjacency matrix. Create the 2D array in two steps: first create a new 1D array of type `bool*`, then for each array element, have it point to a new 1D array of type `bool`. You can then access the array using the 2D notation (e.g., `G->adj[0][1] = true`).

**Note:** Don't ever do this in practice! C has ways of supporting 2D arrays that don't require an extra array of pointers; you'll learn about this more efficient way of doing things in later classes, like 15-213.

(2.c) Complete the functions `graph_hasedge` that checks if an edge is in the graph and `graph_addedge` that adds a new edge to the graph.

(2.d) Complete the `graph_free` function that frees any dynamically-allocated memory for the given graph `G`.

Once you are done implementing the functions above, you should have a complete `graph.c`. Compile your code and test it with the given DFS and BFS searches in `graph-search.c` and the given graphs in `graph-test.c`:

```
% make graphtest
% ./graphtest
```

All tests should pass. (Look at the graphs in `graph-test.c` to see why.) Be sure to use `valgrind` also to make sure you have freed all memory you allocated!

2pt

## Testing for graph connectedness

We say that a graph  $G$  is *fully connected* if there is a path from any vertex to any other vertex in  $G$ . In an undirected graph, this definition is equivalent to saying that there is a path from a *single arbitrary vertex* to any other vertex. Can you see why?

(3.a) Write a function `fully_connected(G)` in `graph-search.c` that returns true if a graph  $G$  is fully connected, or false otherwise. Make sure your implementation is as efficient as possible.

**Hint:** Perform a BFS and count the number of vertices visited. For a fully connected graph, the total should be a specific value. Test your function on several graphs, fully connected and not fully connected.

(3.b) Update `graph-search.h` with the new function, and write at least two test cases in `graph-test.c`: one where `fully_connected` returns true, and one where it returns false.

3pt