Recitation 07: Array Disarray

Thursday February 22nd

Unbounded arrays

When implementing unbounded arrays on an embedded device, a programmer is concerned that doubling the size of the array when we reach its limit may use precious memory resources too aggressively. So she decides to see if she can increase it by a factor of $\frac{3}{2} = 1.5$ instead, rounding down if the result is not an integral number.



This means that it won't make sense for the limit to be less than ______, because otherwise you might resize the array and get an array that wasn't any bigger. This needs to be reflected in the data structure invariant!

```
struct uba_header {
    int size;
2
    int limit;
3
    string[] data;
4
5 };
6 typedef struct uba_header uba;
7
s bool is_arr_expected_length(string[] A, int limit) {
    //@assert \length(A) == limit;
9
    return true;
10
11 }
12
13 bool is_uba(uba* A) {
14
15
16
17 }
```

Checkpoint 0

Implement the function $resize_if_needed(uba* A)$ for this version of unbounded arrays which resizes the array A as described above. Give appropriate preconditions and postconditions, and use an assertion to guard against overflow. (You should not need all the lines provided.)

19	<pre>void resize_if_needed(uba* A)</pre>		
20	//@requires		;
21	//@requires		;
22	//@ensures		;
23	{		
24	if () return;	// No resizing needed
25	assert ();	<pre>// Failure: can't handle bigger!</pre>
26			
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40	}		
41 42 43 44 45 46 47 48 49	<pre>void uba_add(uba* A, string x) //@requires is_uba(A); //@ensures is_uba(A); { A->data[A->size] = x; (A->size)++; resize_if_needed(A);</pre>		
50	}		

Checkpoint 1

Differently from what we did in class, the remaining exercises assume that **each array write costs** \underline{two} **tokens**.



Right after an array resize, we should assume we'll have no tokens in reserve for an array with size k and length 3k/2 (let's assume k is even).

We might have to resize again after as few as _____ uba_add operations.

That next resize would force us to use ______ tokens to copy everything into a larger array (with size 9k/4). The adds that we do in the meantime add elements to the last third of the array, which costs ______ tokens over all operations. Therefore, in total, we need ______ tokens for all uba_add operations.

Each cell in that last third therefore needs to have ______ tokens associated with it.

This gives **uba_add** an amortized cost of ______ tokens.

Checkpoint 2

Repeat this analysis for the case where we triple the size of the array.

We might have to resize again after as few as _____ uba_add operations.

That next resize would force us to use ______ tokens to copy everything into a larger array (with size 9k). The adds that we do in the meantime add elements to the last 2/3 of the array, which costs ______ tokens over all operations. Therefore, in total, we need ______ tokens for all uba_add operations.

Each cell in the last 2/3 therefore needs to have ______ tokens associated with it.

This gives **uba_add** an amortized cost of _____.

Checkpoint 3

Our analysis indicates that a smaller resizing factor gives us a higher amortized cost, even if it's still in O(1). This indicates that doing n operations on this array, while still in O(n), has a higher constant attached to it. Does this make sense?

You will find in the course of your study in algorithms that, like in this example, achieving higher space efficiency often necessitates a tradeoff in time efficiency, and vice versa.