# Database Applications (15-415) 

DBMS Internals- Part VII Lecture 15, March 17, 2014

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## Today...

- Last Session:
- DBMS Internals- Part VI
- Algorithms for Relational Operations
- Today's Session:
- DBMS Internals- Part VII
- Algorithms for Relational Operations (Cont'd)


## DBMS Layers



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## Relational Operations

－We will consider how to implement：
－Selection（ $\sigma$ ）
－Projection $(\pi)$
－Join（ゆゝ）
－Set－difference（一）
－Union（U）
－Aggregation（SUM，MIN，etc．）and GROUP BY
－Since each operation returns a relation，ops can be composed！
－After we cover how to implement operations，we will discuss how to optimize queries（formed by composing operators）

## Assumptions

- We assume the following two relations:

$$
\begin{aligned}
& \text { Sailors (sid: integer, sname: string, rating: integer, age: real) } \\
& \text { Reserves (sid: integer, bid: integer, day: dates, rname: string) }
\end{aligned}
$$

- For Reserves, we assume:
- Each tuple is 40 bytes long, 100 tuples per page, 1000 pages
- For Sailors, we assume:
- Each tuple is 50 bytes long, 80 tuples per page, 500 pages
- Our cost metric is the number of I/Os
- We ignore the computational and output costs


## Outline



## The Join Operation

- Consider the following query, Q , which implies a join:

```
SELECT *
FROM Reserves R, Sailors S
WHERE R.sid = S.sid
```

- How can we evaluate Q ?
- Compute $\mathrm{R} \times \mathrm{S}$
- Select (and project) as required
- But, the result of a cross-product is typically much larger than the result of a join
- Hence, it is very important to implement joins without materializing the underlying cross-product


## The Join Operation

- We will study five join algorithms, two which enumerate the cross-product and three which do not
- Join algorithms which enumerate the cross-product:
- Simple Nested Loops Join
- Block Nested Loops Join
- Join algorithms which do not enumerate the cross-product:
- Index Nested Loops Join
- Sort-Merge Join
- Hash Join


## Assumptions

- We assume equality joins with:
- $\boldsymbol{R}$ represents Reserves and $\boldsymbol{S}$ represents Sailors
- $M$ pages in $\boldsymbol{R}, \boldsymbol{p}_{\boldsymbol{R}}$ tuples per page, $\boldsymbol{m}$ tuples total
- $\boldsymbol{N}$ pages in $\boldsymbol{S}, \boldsymbol{p}_{\boldsymbol{s}}$ tuples per page, $\boldsymbol{n}$ tuples total
- We will consider more complex join conditions later
- Our cost metric is the number of $\mathrm{I} / \mathrm{Os}$
- We ignore output and computational costs


## The Join Operation

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## Simple Nested Loops Join

- Algorithm \#0: (naive) nested loop (SLOW!)



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## for each tuple $r$ of $R$ for each tuple $s$ of $S$ print, if they match



## Simple Nested Loops Join

- Algorithm \#0: (naive) nested loop (SLOW!)


## for each tuple $r$ of $(R)$ for each tuple s of(S) print, if they match



## Simple Nested Loops Join

- Algorithm \#0: (naive) nested loop (SLOW!)

How many disk accesses ( ' M ' and ' $N$ ' are the numbers of pages for ' $R$ ' and ' $S$ ' )?


## Simple Nested Loops Join

- Algorithm \#0: (naive) nested loop (SLOW!)

How many disk accesses ( ' M ' and ' N ' are the numbers of pages for ' $R$ ' and ' $S$ ' )?
$\mathbf{R}(\mathrm{A}, .$.
$\mathrm{I} / \mathrm{O}$ Cost $=\mathrm{M}+\mathrm{m}^{*} \mathrm{~N}$

$\mathbf{S}(\mathrm{A}, \ldots . .$.


## Simple Nested Loops Join

- Algorithm \#0: (naive) nested loop (SLOW!)
- Cost $=\left(p_{R} * M\right) * N+M=100 * 1000 * 500+1000$ I/Os
- At $10 \mathrm{~ms} / \mathrm{IO}$, total $=\sim 6$ days (!)


S(A, ......)

n

Can we do better?

## Nested Loops Join: A Simple Refinement

- Algorithm:
- Read in a page of R
- Read in a page of $S$
- Print matching tuples
$\operatorname{COST}=$ ?



## Nested Loops Join: A Simple Refinement

- Algorithm:
- Read in a page of R
- Read in a page of $S$
- Print matching tuples
$\operatorname{COST}=\mathrm{M}+\mathrm{M}^{*} \mathrm{~N}$



## Nested Loops Join

- Which relation should be the outer?


## $\operatorname{COST}=\mathrm{M}+\mathrm{M} * \mathrm{~N}$



## Nested Loops Join

- Which relation should be the outer?
- A: The smaller (page-wise)

$$
\operatorname{COST}=\mathrm{M}+\mathrm{M} * \mathrm{~N}
$$



## Nested Loops Join

- $\mathrm{M}=1000, \mathrm{~N}=500-$ if larger is the outer:
- Cost $=1000+1000 * 500=501,000$
- = $5010 \mathrm{sec} \sim 1.4 \mathrm{~h}$

$$
\operatorname{cosT}=\mathrm{M}+\mathrm{M} * \mathrm{~N}
$$



## Nested Loops Join

- $\mathrm{M}=1000, \mathrm{~N}=500$ - if smaller is the outer:
- Cost $=500+1000 * 500=500,500$
- $=5005 \mathrm{sec} \sim 1.4 \mathrm{~h}$

$$
\operatorname{COST}=\mathrm{N}+\mathrm{M}^{*} \mathrm{~N}
$$



## Simple Nested Loops Join

- What if we do not apply the page-oriented refinement?
- Cost $=\left(p_{R} * M\right) * N+M=100 * 1000 * 500+1000$ I/Os
- At $10 \mathrm{~ms} / \mathrm{IO}$, total $=\sim 6$ days (!)
- What if we apply the page-oriented refinement?
- Cost $=\mathrm{M}$ * $\mathrm{N}+\mathrm{M}=1000 * 500+1000 \mathrm{I} / \mathrm{Os}$
- At $10 \mathrm{~ms} / \mathrm{IO}$, total $=1.4$ hours (!)
- What if the smaller relation is the outer?
- Slightly better


## The Join Operation

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## Block Nested Loops

- What if we have $B$ buffer pages available?



## Block Nested Loops

- What if we have $B$ buffer pages available?
- A: give B-2 buffer pages to outer, 1 to inner, 1 for output



## Block Nested Loops

- Algorithm:
- Read in $B-2$ pages of R
- Read in a page of $S$
- Print matching tuples

$$
\mathrm{COST}=?
$$



$$
\mathbf{S}(\mathbf{A}, \ldots . . . .)
$$



## Block Nested Loops

- Algorithm:
- Read in $B-2$ pages of R
- Read in a page of $S$
- Print matching tuples

$$
\operatorname{COST}=\mathrm{M}+\mathrm{M} /(\mathrm{B}-2)^{*} \mathrm{~N}
$$



## Block Nested Loops

- And, actually:
- Cost $=\mathrm{M}+\operatorname{ceiling}(\mathrm{M} /(\mathrm{B}-2)) * \mathrm{~N}$

$$
\mathrm{COST}=\mathrm{M}+\mathrm{M} /(\mathrm{B}-2)^{*} \mathrm{~N}
$$



## Block Nested Loops

- If the smallest (outer) relation fits in memory?
- That is, $\mathrm{B}=\mathrm{N}+2$
- Cost $=$ ?



## Block Nested Loops

- If the smallest (outer) relation fits in memory?
- That is, $\mathrm{B}=\mathrm{N}+2$
- Cost $=\mathrm{N}+\mathrm{M}$ (minimum!)



## Nested Loops - Guidelines

- Pick as outer the smallest table (= fewest pages)
- Fit as much of it in memory as possible
- Loop over the inner


## The Join Operation

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## Index Nested Loops Join

- What if there is an index on one of the relations on the join attribute(s)?
- A: Leverage the index by making the indexed relation inner



## Index Nested Loops Join

- Assuming an index on S:
for each tuple $r$ of $R$ for each tuple $s$ of $S$ where $r_{i}==s_{j}$ Add ( $r, s$ ) to result



## Index Nested Loops Join

- What will be the cost?
- Cost: $\mathrm{M}+\mathrm{m}$ * c (c: look-up cost)
' $c$ ' depends on the type of index, the adopted alternative and whether the index is clustered or un-clustered!



## The Join Operation

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## Sort-Merge Join

- Sort both relations on join attribute(s)
- Scan each relation and merge
- This works only for equality join conditions!



## Sort-Merge Join: An Example



## Sort-Merge Join: An Example

| $=$ NO |  |  |  | sid | bid | day | rname |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| sid | sname | rating | age | 8 | 103 | 12/4/4/96 | guppy |
| 22 | dustin | - | 45.0 | 28 | 103 | 11/3/96 | yuppy |
| 28 | yuppy | 9 | 35.0 | 31 | 101 | 10/10/96 | dustin |
| 31 | lubber | 8 | 55.5 | 31 | 102 | 10/12/96 | lubber |
| 44 | guppy | 5 | 35.0 | 31 | 101 | 10/11/96 | lubber |
| 58 | rusty | 10 | 35.0 | 58 | 103 | 11/12/96 | dustin |

## Sort-Merge Join: An Example

| = ? | sid | bid | day | rname |
| :---: | :---: | :---: | :---: | :---: |
|  |  | 103 | 12/4/96 | - |
|  |  | 103 | 11/3/96 | yuppy |
|  |  | 101 | 10/10/96 | dustin |
|  |  | 102 | 10/12/96 | lubber |
|  |  | 101 | 10/11/96 | lubber |
|  |  | 103 | 11/12/96 | dustin |

## Sort-Merge Join: An Example



## Sort-Merge Join: An Example

| $=$ ? | sid | bid | day | rname |
| :---: | :---: | :---: | :---: | :---: |
| ge | 28 | 103 | 12/4/96 | guppy |
| 5.0 | 28 | 103 | $11 / 3 / 96$ | yuppy |
| 0 | 31 | 101 | 10/10/96 | dustin |
| 5.5 | 31 | 102 | 10/12/96 | lubber |
| 35.0 | 31 | 101 | 10/11/96 | lubber |
| 5.0 | 58 | 103 | 11/12/96 | dustin |

## Sort-Merge Join: An Example

| $=\mathrm{YES}$ |  |  |  | sid | bid | day | rname |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| sid | sname | rating | age | 28 | 103 | 12/4/96 | guppy |
| 22 | dustin | 7 | 45.0 |  | 103 | $11 / 3 / 96$ | yuppy |
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## Sort-Merge Join: An Example



## Sort-Merge Join: An Example

$=$ ?


## Sort-Merge Join: An Example

| = NO |  |  |  | sid | bid | day | rname |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
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## Sort-Merge Join: An Example

$=$ ?

| sid | sname | rating | age |
| :---: | :---: | :---: | :---: |
| 22 | dustin | 7 | 45.0 |
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| 31 | lubber | 8 | 55.5 |
| 44 | guppy | 5 | 35.0 |
| 58 | rusty |  | 35. |

## Sort-Merge Join: An Example



## Sort-Merge Join

- What is the cost?
- $\sim 2 * \mathrm{M}^{*} \log \mathrm{M} / \log \mathrm{B}+2 * \mathrm{~N}^{*} \log \mathrm{~N} / \log \mathrm{B}+\mathrm{M}+\mathrm{N}$



## Sort-Merge Join

- Assuming 100 buffer pages, Reserves and Sailors can be sorted in 2 passes
- Total cost = 7500 I/Os
- Cost of Block Nested Loops Join = 7500 I/Os



## Sort-Merge Join

- Assuming 35 buffer pages, Reserves and Sailors can be sorted in 2 passes
- Total cost = 7500 I/Os
- Cost of Block Nested Loops Join = 15000 I/Os



## Sort-Merge Join

- Assuming 300 buffer pages, Reserves and Sailors can be sorted in 2 passes
- Total cost = 7500 I/Os
- Cost of Block Nested Loops Join = 2500 I/Os


It is possible to improve the Sort-Merge Join algorithm by combining the merging phase of sorting with the merging phase of the join!

## Next Class



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